

III. Brightness Temperatures (Radio) - measure of "compactness"

$$T_B = \frac{c^2}{k} \frac{F_\nu}{\nu^2 \Omega}$$

$\Omega =$ solid angle of source as projected on sky

$$= 3.5 \times 10^{12} F_{\nu, Jy} \nu_{GHz}^{-2} \Theta_{mas}^{-2} K$$

⊙ measured with VLBI (Θ_1, Θ_2 if elliptical Gaussian model is used to fit VLBI data, Θ_1, Θ_2 are FWHM size along major + minor axes)

or from variability: $\Theta \approx \frac{c t'_{var, min}}{D} (1+z)^2$

where $t'_{var} = t_{var} \cdot \frac{S}{1+z} \cdot \frac{\langle F_\nu \rangle}{\Delta F_\nu}$

SSC luminosity: $\frac{L_{SSC}}{L_{synch}} \approx \left(\frac{T_B}{2 \times 10^{11} S / (1+z) K} \right)^5 \left(\frac{S}{1+z} \right) \left(\nu_{max} / 10^{11} Hz \right)$
 (Kellermann + Pauliny-Toth 1968)

$\Rightarrow T_B \geq 10^{12} K \cdot \left(\frac{S}{1+z} \right)^{6/5}$ gives $L_{SSC} \gg L_{synch}$ ~ "Inverse Compton catastrophe"

$T_B \approx \text{few} \times 10^{10} K$: equipartition between magnetic + relativistic electron energy densities



Highest measured T_B : 3C 279 (VLBI with space antenna) = $2 \times 10^{13} K$
 0408-379 (scintillation) = $2 \times 10^{14} K$
 not sure of name \uparrow requires distance of scattering "screen" - T_B lower if distance $\sim 5-10 pc$
 problematic (some coherent emission process?) $T \sim \text{few } 100 ?$

IV. Polarization

A. Linear: synchrotron radiation $\Pi \approx \frac{3(\alpha+1)}{3\alpha+5} \frac{B_{unif}^2}{B_{unif}^2 + B_{rand}^2}$ 0.72 for $\alpha=0.7$

(Burn 1966, MNRAS, 133, 67)

Observed: most jet features have $\Pi \approx 10\% \rightarrow B_{rand} \sim 2.5 B_{unif}$

Direction = electric vector position angle (EVPA) \perp projected $\langle \vec{B} \rangle$.
 - But optically thick case: $\Pi \approx 0.05, \chi \parallel \vec{B}_{proj}$
 Shock: Component of B that is \parallel shock front is amplified \Rightarrow EVPA $\rightarrow \perp$ shock front
 Face-on:  Fairly random
 Edge-on:  \uparrow net \vec{B} direction
 $\Theta \approx \sin^{-1}(\gamma \beta)$